

## ICS Problem Sheet #2

**Problem 2.1:** *proof by contrapositive*

(4 points)

Let  $n$  be a natural number. If  $n^2$  is divisible by 3, then  $n$  is divisible by 3.

Prove this statement by proving the contrapositive. (You may want to consider different cases how a number not divisible by 3 can be written.)

**Problem 2.2:** *proof by induction*

(6 points)

Let  $n$  be a natural number. Proof that the following is true:

$$0^3 + 1^3 + 2^3 + \dots + n^3 = \sum_{i=0}^n i^3 = \left[ \frac{n(n+1)}{2} \right]^2$$