## ICS 2021 Problem Sheet \#7

Problem 7.1: quine-mccluskey algorithm
Consider integer numbers in the range $0 . . .63$ that can be represented using six bits. The boolean function $F\left(X_{5}, X_{4}, X_{3}, X_{2}, X_{1}, X_{0}\right)$ is true when the number $\left(X_{5} X_{4} X_{3} X_{2} X_{1} X_{0}\right)_{2}$ is a Fibonacci number and false otherwise.
a) Provide a boolean expression in DNF defining the function $F$. What is the cost of the DNF expression?
b) Calculate the prime implicants of $F$.
c) Construct the prime implicant chart and identify the essential prime implicants. What is a minimal set of prime implicants covering the function $F$ ?
d) Write out a minimal boolean expression defining $F$ using mathematical logic notation. What is the cost of the minimal boolean expression?

For calculating the cost of a boolean expression, we only consider logical $\wedge$ and $\vee$ operations.

