

OS 2022 Problem Sheet #3

Problem 3.1: readers / writers problem

(1+1+1 = 3 points)

Below are three incorrect solutions of the readers-writers problem. Explain why the solutions works or in which situations the solutions fail to work correctly. The solutions use the following common definitions:

```
shared object data;
shared int readcount = 0;
semaphore mutex = 1, writer = 1;
```

a) void reader() { down(&mutex); readcount = readcount + 1; if (readcount == 1) down(&writer); up(&mutex); read_shared_object(&data); down(&mutex); readcount = readcount - 1; up(&mutex); if (readcount == 0) up(&writer); }	void writer() { down(&writer); write_shared_object(&data); up(&writer); }
b) void reader() { down(&mutex); readcount = readcount + 1; if (readcount == 1) down(&writer); up(&mutex); read_shared_object(&data); down(&mutex); readcount = readcount - 1; if (readcount == 0) { up(&mutex); up(&writer); } else { up(&mutex); } }	void writer() { down(&writer); write_shared_object(&data); up(&writer); }
c) void reader() { down(&mutex); readcount = readcount + 1; if (readcount == 1) down(&writer); up(&mutex); read_shared_object(&data); down(&mutex); readcount = readcount - 1; if (readcount == 0) up(&writer); up(&mutex); }	void writer() { down(&writer); down(&mutex); write_shared_object(&data); up(&mutex); up(&writer); }

Problem 3.2: perfect numbers (multi-threading)

(2+3+2 = 7 points)

A *perfect number* is a positive integer that is equal to the sum of its positive divisors, excluding the number itself. For example, 6 has the positive divisors { 1, 2, 3 } and $1 + 2 + 3 = 6$.

Write a C program called `perfect` that finds perfect numbers in a range for numbers. The default number range is [1,10000]. The program accepts the `-s` option to set the lower bound and the `-e` option to set the higher bound. Hence, the invocation `perfect -s 100 -e 1000` will search for perfect numbers in the range [100,1000].

The following function can be used to test whether a given number is a perfect number:

```
#include <stdint.h>

static int
is_perfect(uint64_t num)
{
    uint64_t i, sum;

    if (num < 2) {
        return 0;
    }

    for (i = 2, sum = 1; i*i <= num; i++) {
        if (num % i == 0) {
            sum += (i*i == num) ? i : i + num / i;
        }
    }

    return (sum == num);
}
```

- a) Write a program that searches for perfect numbers in a range of numbers. Your program must support the `-s` and `-e` options to define non-default search intervals.

```
./perfect -s 100 -e 10000
496
8128
```

- b) Implement an option `-t` that can be used to define how many concurrent threads should be used to execute the search. If the `-t` option is not present, then a single thread is used to carry out the search. For debugging purposes, implement an option `-v` that writes trace information to the standard error. Below is an invocation with two threads and a verbose trace.

```
./perfect -t 2 -v
perfect: t0 searching [1,5000]
perfect: t1 searching [5001,10000]
6
28
496
8128
perfect: t0 finishing
perfect: t1 finishing
```

- c) Determine how the `-t` option impacts the execution time. Pick a search interval that is a reasonable load for your computer hardware and then increase the threading level and determine how the execution time changes. Produce a plot presenting the measurements you have obtained and discuss the results.