

### SADS 2018 Problem Sheet #3

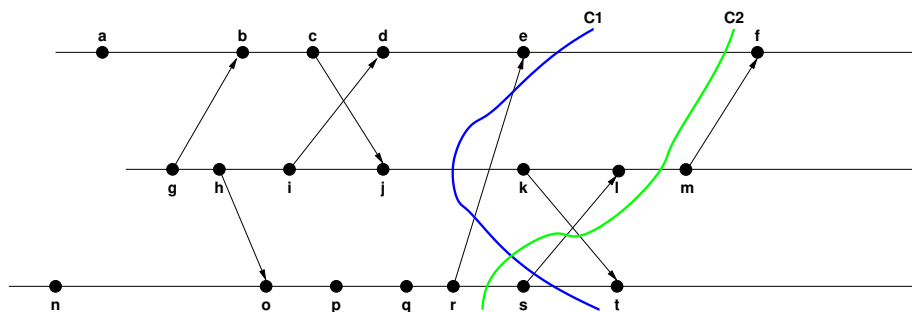
**Problem 3.1:** *lambport clocks and vector clocks* (1+1+1 = 3 points)

Let  $e \prec f$  (with  $e, f \in E$ ) be the causal order relation on the set of events  $E$  with  $n$  concurrent processes. Let  $\Theta_L : E \mapsto \mathbb{N}$  denote a Lamport clock and  $\Theta_V : E \mapsto \mathbb{N}^n$  denote a vector clock.

- a) Given two events  $e, f \in E$  with  $e \neq f$  and with  $\Theta_L(e) < \Theta_L(f)$ , which of the following statements are true or false? Provide a reasoning.
  - (i)  $\Theta_L(e) < \Theta_L(f) \implies e \prec f$
  - (ii)  $\Theta_L(e) < \Theta_L(f) \implies f \prec e$
- b) Given two events  $e, f \in E$  with  $e \neq f$  and with  $\Theta_V(e) < \Theta_V(f)$ , which of the following statements are true or false? Provide a reasoning.
  - (i)  $\Theta_V(e) < \Theta_V(f) \implies e \prec f$
  - (ii)  $\Theta_V(e) < \Theta_V(f) \implies f \prec e$
- c) Given two concurrent events  $e, f \in E$  with  $e \neq f$ . How can one determine from the vector clock values  $\Theta_V(e)$  and  $\Theta_V(f)$  that  $e$  and  $f$  are concurrent?

**Problem 3.2:** *logical clocks and consistent cuts* (2+2+1 = 5 points)

Consider a distributed system with three processes that proceeds as shown below:



- a) Determine the Lamport clock values for all events.
- b) Determine the vector clock values for all events.
- c) Are the cuts  $C_1$  and  $C_2$  consistent cuts? Explain why or why not.

**Problem 3.3:** *unisex bathroom problem using communicating sequential processes* (2 points)

The university agreed to establish unisex bathrooms, provided that the following constraints can be maintained:

- There cannot be men and women in the bathroom at the same time.
- There should never be more than three students squandering time in the bathroom.

Model the situation using communicating sequential processes for  $N$  female students and  $M$  male students. Make sure your definitions are both syntactically and semantically correct.