

SADS 2021 Problem Sheet #6

Problem 6.1: substitution-permutation network

(7+1+1+1 = 10 points)

We define a substitution-permutation network implementing an 8-bit block cipher with keys of a length of 32 bits. We call this cipher *sads crypt*, or short *scrypt*.

- The key step takes 8 bits from the key and performs a bitwise exclusive or with current 8-bit value.
- The substitution step uses 4-bit S-boxes applied to the lower and upper 4 bits of an 8-bit word. The substitution $S : \{0, 1\}^4 \rightarrow \{0, 1\}^4$ is given by $x \mapsto ((x + 1) \cdot 7) \bmod (17 - 1)$. This is a bijection of $\{0, 1\}^4$, where 4-bit chunks are seen as natural numbers via their binary encoding.
- The permutation step uses an 8-bit P-box $P : \{0, 1\}^8 \rightarrow \{0, 1\}^8$, which does a cyclic 2-bit left-shift of its argument.

The substitution-permutation network uses the following rounds:

- Round 0: Key step with the first (most significant) 8 bits of the key.
 - Round 1: Substitution step followed by a permutation step followed by a key step with the next 8 bits of the key.
 - Round 2: Substitution step followed by a permutation step followed by a key step with the next 8 bits of the key.
 - Round 3: Substitution step followed by a key step with the last (least significant) 8 bits of the key.
- a) Write a file `scrypt.c` implementing the public interface defined by `scrypt.h`. We provide you with unit tests so that you can check your implementation. Consider implementing the S-boxes and P-boxes as internal helper functions.
 - b) Encrypt the cleartext “secret” (0x736563726574) in electronic codebook mode with the key 0x98267351.
 - c) Encrypt the cleartext “hacker” (0x6861636b6572) in cipher block chaining mode with the key 0x98267351 and the initialization vector 0x42.
 - d) Decrypt the ciphertext 0xc65e05946b86eb2e33f58fdaff0f42, which has been produced using cipher block chaining mode with the key 0x98267351 and the initialization vector 0x42.

Below is the `scrypt.h` header file defining the public interface. To answer the questions b)-d), you may want to implement a small main program that allows you to play with your *scrypt* implementation.

```

/*
 * scrypt/src/scrypt.h --
 */

#ifdef _SCRYPT_H
#define _SCRYPT_H

#include <stdint.h>

/**
 * \brief Encrypt an 8-bit cleartext using a 32-bit key.
 *
 * \param m 8-bit cleartext.
 * \param k 32-bit key.
 * \result 8-bit ciphertext.
 */

uint8_t
sc_enc8(uint8_t m, uint32_t k);

/**
 * \brief Decrypt an 8-bit ciphertext using a 32-bit key.
 *
 * \param m 8-bit ciphertext.
 * \param k 32-bit key.
 * \result 8-bit cleartext.
 */

uint8_t
sc_dec8(uint8_t c, uint32_t k);

/**
 * \brief Encrypt a variable-length cleartext using a 32-bit key in ECB mode.
 *
 * \param m cleartext.
 * \param c ciphertext.
 * \param len length of the cleartext and ciphertext buffers.
 * \param k 32-bit key.
 */

void
sc_enc_ecb(unsigned char *m, unsigned char *c, size_t len, uint32_t k);

/**
 * \brief Decrypt variable-length ciphertext using a 32-bit key in ECB mode.
 *
 * \param c ciphertext.
 * \param m cleartext.
 * \param len length of the ciphertext and cleartext buffers.
 * \param k 32-bit key.
 */

void
sc_dec_ecb(unsigned char *c, unsigned char *m, size_t len, uint32_t k);

/**
 * \brief Encrypt a variable-length cleartext using a 32-bit key in CBC mode.
 *
 * \param m cleartext.
 * \param c ciphertext.
 * \param len length of the cleartext and ciphertext buffers.
 * \param k 32-bit key.
 * \param iv 8-bit initialization vector.
 */

```

```
*/

void
sc_enc_cbc(unsigned char *m, unsigned char *c, size_t len,
           uint32_t k, uint8_t iv);

/**
 * \brief Decrypt variable-length ciphertext using a 32-bit key in CBC mode.
 *
 * \param m ciphertext.
 * \param m cleartext.
 * \param len length of the ciphertext.
 * \param k 32-bit key.
 * \param iv 8-bit initialization vector.
 */

void
sc_dec_cbc(unsigned char *c, unsigned char *m, size_t len,
           uint32_t k, uint8_t iv);

#endif
```